

Query Stability in Data-aware Business Processes*

Ognjen Savković



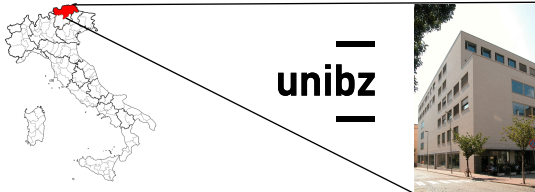
Free University of Bozen-Bolzano

joint work with
Elisa Marengo and Werner Nutt

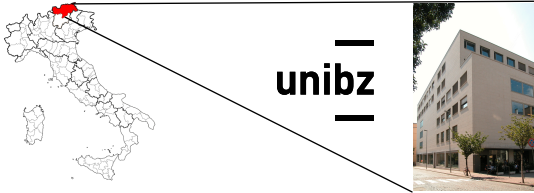
EPCL PhD Workshop, April 2014, Dresden

*Supported by the project MAGIC, funded by the Province of Bozen-Bolzano

Students at Free University of Bozen-Bolzano (FUB)

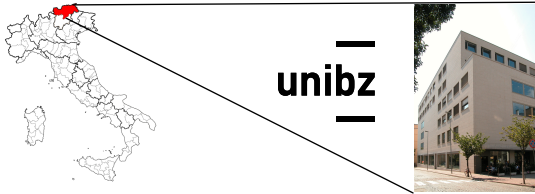


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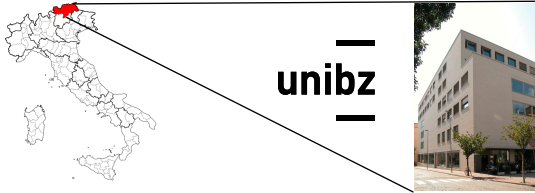
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Statistical Report about the Enrolled Students at FUB

Faculty of Economics	Student places 2012 / 2013	Enrollments 2011 / 2012	Enrollments 2012 / 2013	%
Bachelor in Economics and Management	110	27	21	20.78%
Bachelor in Tourism, Sport and Event Management	110	31	80	74.51%
Bachelor in Economics and Social Sciences	110	23	24	17.24%
Master in Entrepreneurship and Innovation	110	11	10	114.29%
Master in Economics and Management of the public sector	110	20	27	22.73%
Sum	370	193	273	41.45%

Faculty of Computer Science	Student Places 2012 / 2013	Enrollments 2011 / 2012	Enrollments 2012 / 2013	%
Bachelor in Computer Science and Engineering	110	23	30	30.43%
Master of Science in Computer Science	80	30	20	-44.44%
PhD in Computer Science	10	0	0	#VALUE!
Sum	200	53	50	-25.37%

How Reliable are the Figures in the Report?

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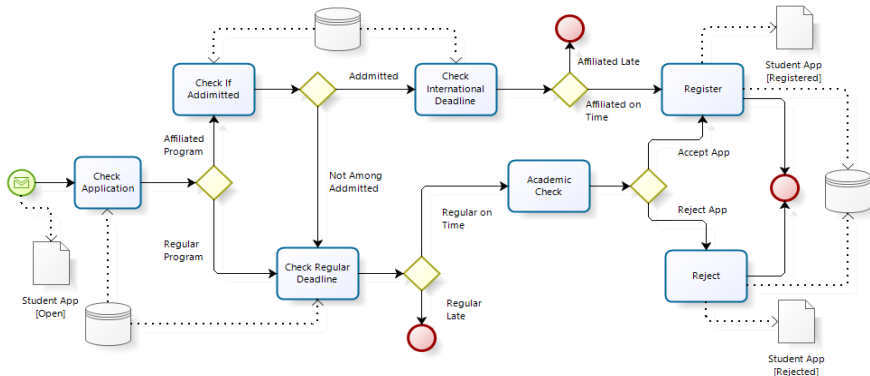


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Look at the **Business Processes** that **generates** and **manipulates data**.

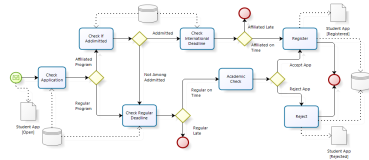
Student Registration Processes at FUB



What are Business Processes (BPs)?

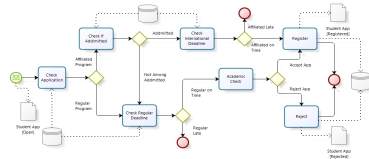
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 - e.g., **student registration process**



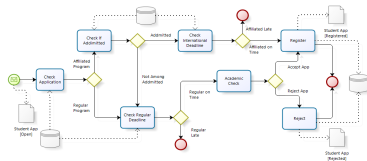
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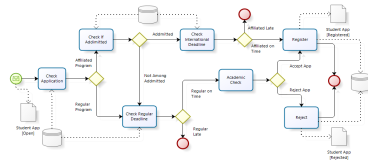


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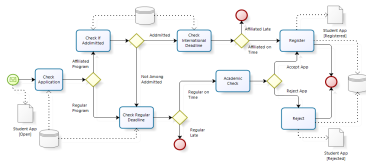


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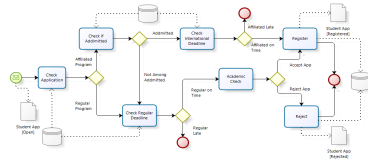


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- BPs **fail to model** interaction with **databases**
 - Formal BPs models, e.g. *Petri Nets*, traditionally **represent data in a limited way**
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 - In BPEL operations on the database are **hidden in the code**
- However, **data** is often the **main driver** when **executing BPs**
 - E.g., **a student can register for a program**
only if the student was firstly admitted to the program

Property of Query Stability

Query Stability

Informally, that is when for a given query Q and a business process \mathcal{B} that manipulates data the **query answer** of Q **does not change** for all future transformations of data according to \mathcal{B} .

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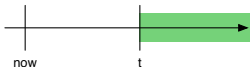
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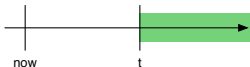
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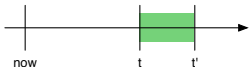
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- What are the **time intervals** in which Q is stable?



Outline

Data-aware Business Processes (DABPs) model

Query Stability

Reasoning about Query Stability in DABPs

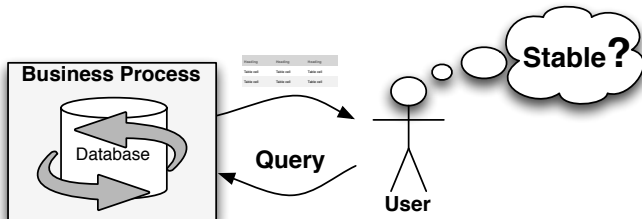


Table of Contents

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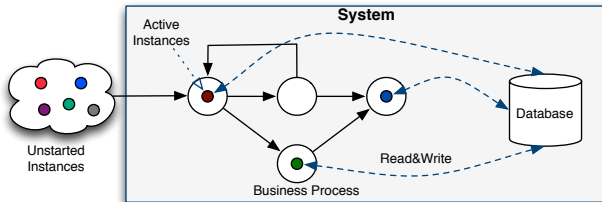
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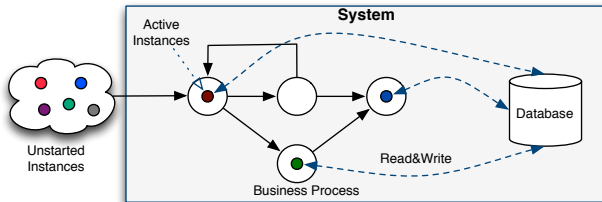
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New Information in the system is brought with **new process instances**

Process Part in DABPs

- Process Part $\mathcal{P} = \langle N, L \rangle$ is defined with **process net** N and **data rules** L

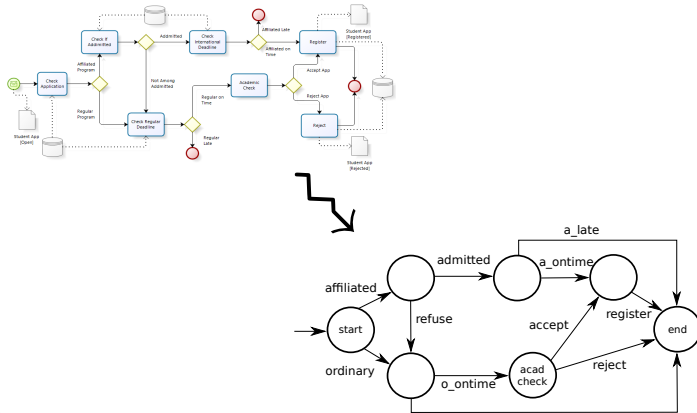
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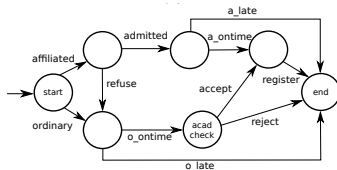
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- Here, E_t and Q_t are **CQ with safe negation** over signature $\Sigma \cup I$ and $R \in \Sigma$
- Relation I is the input relation that describes process instance
 - e.g., **student application form** $I('J. Smith', 'EMCL', 'Thursday 20^{th}$ October, 2016')
 - (the last I -argument is reserved for the instance timestamp)

Running example: process part



Transition	Execution Condition E_t
affiliated	$I(s, p, \tau), \text{StudyPlan}(p, \text{'affil'}, m)$
ordinary	$I(s, p, \tau), \text{StudyPlan}(p, \text{'ord'}, m), \neg \text{StudyPlan}(s, \text{'affil'}, p)$
admitted	$I(s, p, \tau), \text{Admitted}(s, p)$
refuse	$I(s, p, \tau), \text{Admitted}(s, p), \text{StudyPlan}(p, \text{'ord'}, m)$
a_late	$I(s, p, \tau), \text{Deadline}(\text{'affil'}, d), \tau > d$
a_ontime	$I(s, p, \tau), \text{Deadline}(\text{'affil'}, d), \tau < d$
o_late	$I(s, p, \tau), \text{Deadline}(\text{'affil'}, d), \tau > d$
o_late	$I(s, p, \tau), \text{Deadline}(\text{'ord'}, d), \tau > d$
o_ontime	$I(s, p, \tau), \text{Deadline}(\text{'ord'}, d), \tau < d$
Writing Rule W_t	
register	$I(s, p, \tau), \text{StudyPlan}(p, r, m) \rightarrow \text{Registered}(s, m, p)$

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- **Database instance** D over schema Σ
- Set of **process instances** O (called **data objects**)
- **Mapping function** M that for every data object $o \in O$ determines **current place** in the process $M_P(o) = p \in P$ and a single I -record $M_S(o) = I(\bar{s})$ of the input relation $I \notin \Sigma$
- **Current timestamp** τ of the configuration

Running Example: Initial Configuration

- Database instance *D*

<i>StudyPlan</i>		
<i>program</i>	<i>registr.</i>	<i>master</i>
emSE	<i>affil</i>	mscCS
emCL	<i>affil</i>	mscCS
emCL	<i>reg</i>	mscCS
econ	<i>reg</i>	mscECO

<i>Admitted</i>	
<i>student</i>	<i>program</i>
bob	emCL
mary	emSE

<i>Deadline</i>	
<i>registr.</i>	<i>date</i>
<i>reg</i>	1 st Oct
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Running Example: Initial Configuration

- Database instance D
- Data objects $O = \{o_1, o_2, o_3\}$

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- Mapping M

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o_3	(john, db, τ_3)	<i>start</i>
o_2	(alice, econ, τ_2)	<i>end</i>
o_1	(bob, emCL, τ_1)	<i>end</i>

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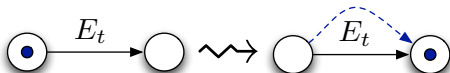
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- Current time
 $\tau = \text{'Thursday 20th October, 2016'}$

Execution of DABPs

There are two kinds of **atomic execution** in DABPs

- **Traversal** of a transition in the net by an object

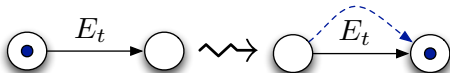


An object o with I -record $I(\bar{s})$ can traverse transition t if $E_t(D \cup I(\bar{s})) = true$
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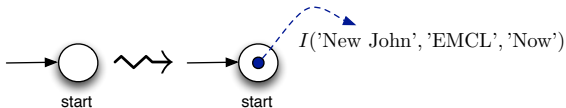
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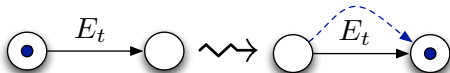


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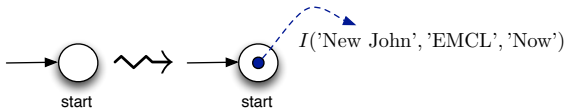
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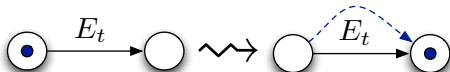
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- In both cases a **new configuration** $\mathcal{C}' = \langle D', O', M', \tau' \rangle$ is obtained as a result

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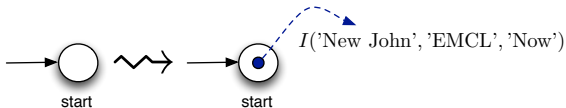
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- **Traversal** of a transition in the net by an object



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 + the **database instance** is updated so $D' = D \cup W_t(D \cup I(\bar{s}))$

- **Introduction** of a fresh object o with a fresh I -record



+ the **configuration timestamp** τ' is set to be the timestamps of o

- In both cases a **new configuration** $\mathcal{C}' = \langle D', O', M', \tau' \rangle$ is obtained as a result
- **Executions** in DABPs are finite sequences of atomic executions

Table of Contents

Data-aware Business Processes (DABPs) model

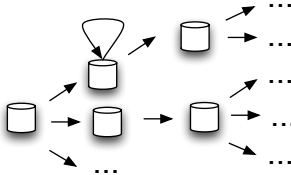
Query Stability

Reasoning about Query Stability in DABPs

Query Stability Formally

- Query Q is **stable** in DABP $\mathcal{B} = \langle \mathcal{P}, \mathcal{C} \rangle$ with database D if for any *reachable* configuration with the database D'

$$Q(D) = Q(D')$$



Running Example: Stability of Queries

- Q_{CS} : Who are the registered students at the Faculty of Computer Science?
e.g., $Q_{CS}(x) \leftarrow Registered(x, 'mscCS', p)$
- Q_{eco} : Who are the registered students at the Faculty of Economics?
e.g., $Q_{eco}(x) \leftarrow Registered(x, 'mscECO', p)$

Faculty of Economics	Student places 2012 / 2013	Enrollments 2011 / 2012	Enrollments 2012 / 2013	%	Stable?	< 1st Oct	1st Oct-1st Dec	> 1st Dec
Bachelor in Economics and Management	20	28	20	20,78%		NO!	YES!	YES!
Bachelor in Tourism, Sport and Event Management	74	51	74	74,51%		NO!	YES!	YES!
Bachelor in Economics and Social Sciences	17	24	17	17,24%		NO!	YES!	YES!
Master in Entrepreneurship and Innovation	114	29	114	114,29%		NO!	YES!	YES!
Master in Economics and Management of the public sector	22	73	22	22,73%		NO!	YES!	YES!
Sum	247	205	247	41,45%		NO!	YES!	YES!
Faculty of Computer Science	Student Places 2012 / 2013	Enrollments 2011 / 2012	Enrollments 2012 / 2013	%		< 1st Oct	1st Oct-1st Dec	> 1st Dec
Bachelor in Computer Science and Engineering	30	43	30	30,43%		NO!	YES!	YES!
Master of Science in Computer Science	-44	44	-44	-44,44%		NO!	NO!	YES!
PhD in Computer Science	#VALUE!			#VALUE!		NO!	NO!	YES!
Sum	13	87	20	-25,37%		NO!	NO!	YES!

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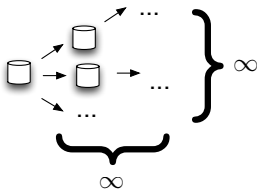
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- **Process Rules: Normal(w/ negation) or or Positive(w/o negation)**

How complex is to check stability for Conjunctive Queries

- **Undcidable** in the most general case :(
even in the **data** and **query** complexity

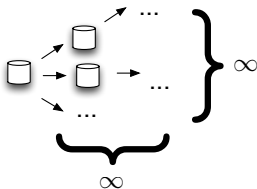
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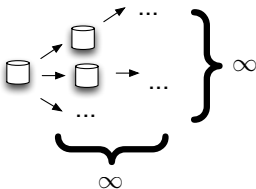
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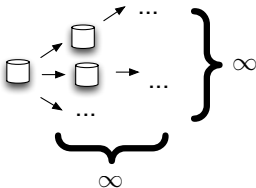
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- Still, many **decidable** cases :) by restricting DAPBs to
 - **closed semantics** (no fresh instances are allowed, so obvious :)
 - **positive rules** (little less obvious)

How complex is to check stability for Conjunctive Queries

Process Rules	Process Net	Semantics	Configuration	Data	Process	Query	Combined
<i>Normal</i>	<i>Cyclic / Acyclic</i>	<i>Open</i>	<i>Arbitrary</i>	UNDEC.	UNDEC.	UNDEC.	UNDEC.
	<i>Cyclic / Acyclic</i>	<i>Open</i>	<i>Fresh</i>	UNDEC.	UNDEC.	UNDEC.	UNDEC.
	<i>Cyclic</i>	<i>Closed</i>	<i>Arbitrary</i>	CO-NP	CO-NEXPTIME	Π_2^P	CO-NEXPTIME
	<i>Acyclic</i>	<i>Closed</i>	<i>Arbitrary</i>	CO-NP	PSPACE	Π_2^P	PSPACE
<i>Positive</i>	<i>Cyclic / Acyclic</i>	<i>Open</i>	<i>Arbitrary</i>	CO-NP	EXPTIME	Π_2^P	EXPTIME
	<i>Cyclic / Acyclic</i>	<i>Open</i>	<i>Fresh</i>	PTIME	EXPTIME	Π_2^P	EXPTIME
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Encoding techniques for decidable DABPs

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Let $\omega = o_1, t_1, o_2, t_2, \dots, o_n, t_n$ be an execution in \mathcal{B} . Then one can construct a Datalog program $\Pi_{\mathcal{B}}$ such that

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- $\Pi_{\mathcal{B}} \models_{\text{brave}} \tilde{R}_1(\bar{\omega}, \bar{s}_1), \dots, \tilde{R}_n(\bar{\omega}, \bar{s}_n)$

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Compute all executions using **nonrecursive** **Datalog** (**PSPACE**)



Can we obtain interesting **tractable** cases?

Read-Only Write-only DAPBs

- Split schema Σ into **Read-only** schema Σ_R and **Write-Only** schema Σ_W

Read-Only Write-only DAPBs

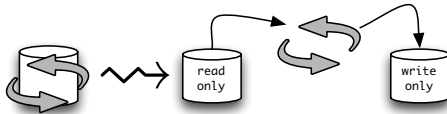
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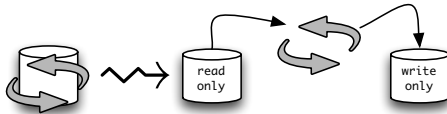
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- *Thus, objects cannot read what they have written*

Checking stability in Read-Only Write-only DAPBs

- nicer complexities :)

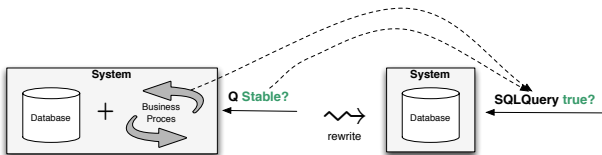
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- Checking Stability in rowo DABPs is **FO-rewritable**



Future Work

We plan to consider

- *More expressive queries*, e.g., CQ with negation or FO;
- *Stability of aggregate queries / aggregates in the process rules*;
- *Quantify instability*,
e.g., compute the minimal/maximal number of new answers;
- Other data quality aspects such as *data timeliness* and *data currency*.

Thank you!

